

## Day 7 – Equations of Circles

A circle is the set of all points  $(x, y)$  in a plane that are equidistant from a fixed point called the center of the circle. The distance between the center and any point  $(x, y)$  on the circle is called the radius.

The Standard Form of a Circle

Centered at the Origin:

$$x^2 + y^2 = r^2$$

$(0, 0)$  is the center

$r$  is the radius

The Standard Form of a Circle

Centered Not at the Origin:

$$(x - h)^2 + (y - k)^2 = r^2$$

$(h, k)$  is the center

$r$  is the radius

The General Form of a Circle:

$$Ax^2 + By^2 + Cx + Dy + E = 0$$

Name: \_\_\_\_\_

$$(x-h)^2 + (y-k)^2 = r^2$$

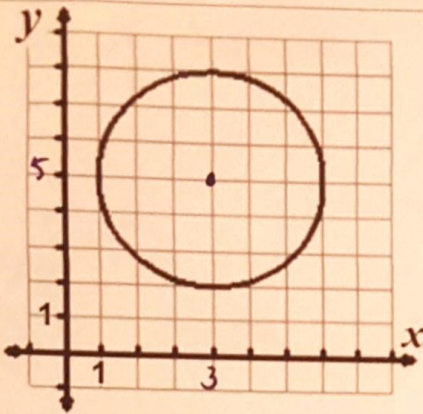
 $(h, k) = \text{center}$   
Date: \_\_\_\_\_

$$\sqrt{r^2} = r$$

## WRITING CIRCLE EQUATIONS FROM GRIDS

For #1-12, write the coordinates  $(h, k)$  of the center point, the radius length and the equation of each circle.

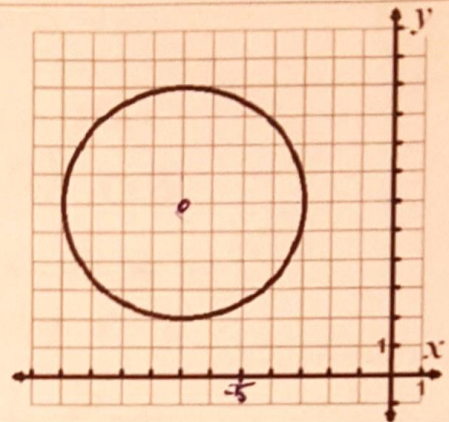
①

Center  $(h, k) = (3, 5)$ Radius = 3

Equation:

$$(x-3)^2 + (y-5)^2 = 9$$

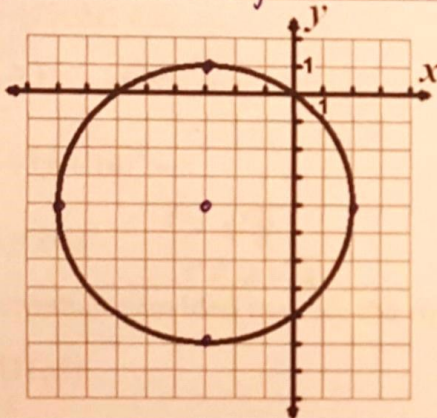
②

Center  $(h, k) = (-7, 6)$ Radius = 4

Equation:

$$(x+7)^2 + (y-6)^2 = 16$$

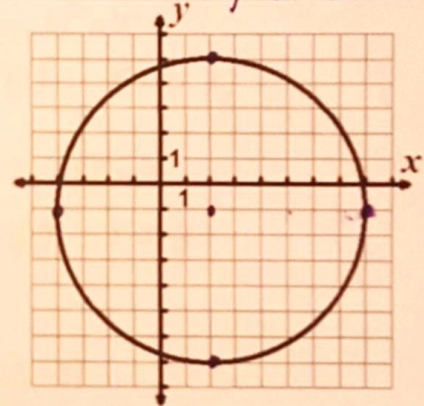
③

Center  $(h, k) = (-3, -4)$ Radius = 5

Equation:

$$(x+3)^2 + (y+4)^2 = 25$$

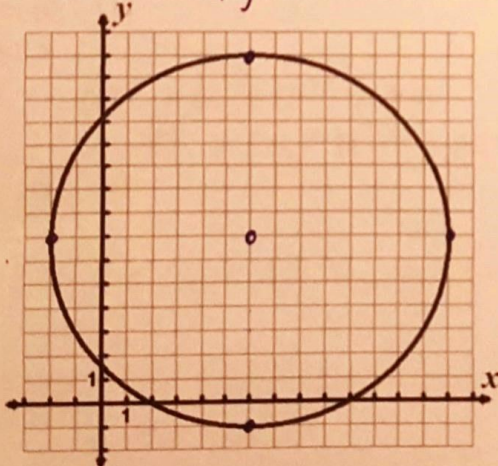
④

Center  $(h, k) = (2, -1)$ Radius = 6

Equation:

$$(x-2)^2 + (y+1)^2 = 36$$

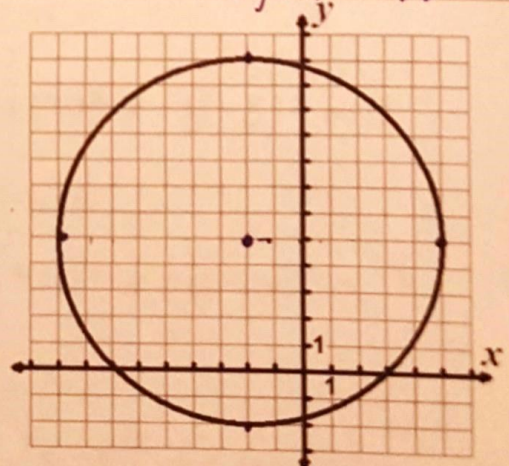
⑤

Center  $(h, k) = (6, 7)$ Radius = 8

Equation:

$$(x-6)^2 + (y-7)^2 = 64$$

⑥

Center  $(h, k) = (-2, 5)$ Radius = 7

Equation:

$$(x+2)^2 + (y-5)^2 = 49$$

## Equations of Circles

Identify the center and radius of each.

1)  $(x-9)^2 + (y-6)^2 = 4$

C: (9, 6)      r: 2

2)  $(x+4)^2 + (y-12)^2 = 9$

C: (-4, 12)      r = 3

3)  $(x+9)^2 + (y+4)^2 = 95$

C: (-9, -4)      r:  $\sqrt{95}$

4)  $(x+8)^2 + (y-4)^2 = 36$

C: (-8, 4)      r = 6

5)  $(x-7)^2 + (y+11)^2 = 25$

C: (7, -11)      r = 5

6)  $(x+10)^2 + (y-5)^2 = 41$

C: (-10, 5)      r =  $\sqrt{41}$

7)  $(x-4)^2 + (y-3)^2 = 81$

C: (4, 3)      r = 9

8)  $(x+3)^2 + (y-8)^2 = 77$

C: (-3, 8)      r =  $\sqrt{77}$

9)  $(x-16)^2 + (y+14)^2 = 8$

C: (16, -14)      r =  $\sqrt{8}$   
r =  $2\sqrt{2}$

10)  $(x-15)^2 + (y+8)^2 = 9$

C: (15, -8)      r = 3

Use the information provided to write the equation of each circle.

11) Center: (11, 2)

Radius: 6

$(x-11)^2 + (y-2)^2 = 36$

12) Center: (-12, -5)

Radius: 4

$(x+12)^2 + (y+5)^2 = 16$

13) Center: (0, -11)

Radius: 5

$(x-0)^2 + (y+11)^2 = 25$   
 $x^2 + (y+11)^2 = 25$

14) Center: (-15, 8)

Radius: 3

$(x+15)^2 + (y-8)^2 = 9$

15) Center: (1, -15)

Radius: 3

$(x-1)^2 + (y+15)^2 = 9$

16) Center: (-3, 16)

Radius: 3

$(x+3)^2 + (y-16)^2 = 9$

17) Center: (6, 0)

Radius: 7

$(x-6)^2 + (y-0)^2 = 49$   
 $(x-6)^2 + y^2 = 49$

18) Center: (1, 7)

Radius: 7

$(x-1)^2 + (y-7)^2 = 49$

19) Center: (10, 10)

Radius: 3

$(x-10)^2 + (y-10)^2 = 9$

20) Center: (-11, 13)

Radius: 5

$(x+11)^2 + (y-13)^2 = 25$