

Given the polynomials below, identify the y-intercept.

1. $f(x) = 3x^3 + 2x^2 - 6x - 1$

(0, -1)

2. $f(x) = -4x^4 - 5x^3 + 2x^2 + 4x + 5$

(0, 5)

How many solutions does the polynomial below have? Also, identify the degree and name the function.

3. $f(x) = -2x^3 + 6x^2 - 5x + 3$

of solutions: 3

Degree: 3

Name of function: Cubic

4. $f(x) = 2x^4 + x^3 - x^2 + 4x + 3$

of solutions: 4

Degree: 4

Name of function: Quartic

Write the polynomial function in factored form that has zeros:

5. 1, -2, 5

$(x-1)(x+2)(x-5)$

6. 4, 3i, -3i

$(x-4)(x-3i)(x+3i)$

7. 0, -1, -6, 9

- a) $x(x-1)(x-6)(x+9)$
- b) $x(x+1)(x+6)(x-9)$
- c) $x(x-1)(x+6)(x+9)$
- d) $x(x+1)(x-6)(x-9)$

Find all zeros of the polynomial function. One factor has been given

8. $x^3 - 7x^2 - 9x + 63 = 0$; $x + 3$

$a=1, b=-7, c=-9, d=63$ poly solve # 2

a) $x = -3, x = 3, x = 7$

b) $x = 3, x = -3, x = -7$

c) $x = -3, x = -3, x = 7$

d) $x = -3, x = -3, x = -7$

9. $2x^3 - 23x^2 + 85x - 100 = 0$; $x - 5$

poly solve #

a) $x = 5, x = 4, x = 5/2$

b) $x = -5, x = -4, x = -5/2$

c) $x = 5, x = -4, x = 5/2$

d) $x = -5, x = 4, x = -5/2$

10. $3x^3 - 2x^2 - 61x - 20 = 0$; $x + 4$

$$\begin{array}{r|rrrr} -4 & 3 & -2 & -61 & -20 \\ & \downarrow & & & \\ & & -12 & 56 & 20 \\ \hline & 3 & -14 & -5 & 0 \end{array}$$

$x = 5$

$x = -1/3$

$x = -4$

$3x^2 - 14x - 5 = 0$

$(x-5)(x+1) = 0$

$x^2 - 14x - 15 = 0$

$(x-5)(x+3) = 0$

11. $x^3 - 10x^2 + 31x - 30 = 0$; $x - 2$

$$\begin{array}{r|rrrr} 2 & 1 & -10 & 31 & -30 \\ & \downarrow & & & \\ & & 2 & -76 & 36 \\ \hline & 1 & -8 & 15 & 0 \end{array}$$

$x^2 - 8x + 15 = 0$

$(x-5)(x-3) = 0$

$x = 2, x = 5, x = 3$

Find all zeros of the polynomial function. One zero has been given

12. $2x^3 - 7x^2 + 2x + 3 = 0$; 3

$$\begin{array}{r|rrrr} 3 & 2 & -7 & 2 & 3 \\ & \downarrow & & & \\ & & 6 & -3 & -3 \\ \hline & 2 & -1 & -1 & 0 \end{array}$$

$2x^2 - 1x - 1 = 0$

$(x-2)(x+1) = 0$

$x^2 - 1x - 2 = 0$

$x = 1, x = -1/2, x = 3$

13. $x^3 + 7x^2 + 2x - 40 = 0$; -5

$$\begin{array}{r|rrrr} -5 & 1 & 7 & 2 & -40 \\ & \downarrow & & & \\ & & -5 & -10 & 40 \\ \hline & 1 & 2 & -8 & 0 \end{array}$$

$x^2 + 2x - 8 = 0$

$(x-2)(x+4) = 0$

$x = -5, x = 2, x = -4$

14. $x^3 - 5x^2 - 9x + 45 = 0$; 5

poly solve #

a) $x = 5, x = 3, x = -3$

b) $x = 5, x = 3, x = 3$

c) $x = -5, x = -3, x = -3$

d) $x = -5, x = 3, x = -3$

15. $x^3 + x^2 - 17x + 15 = 0$; -5

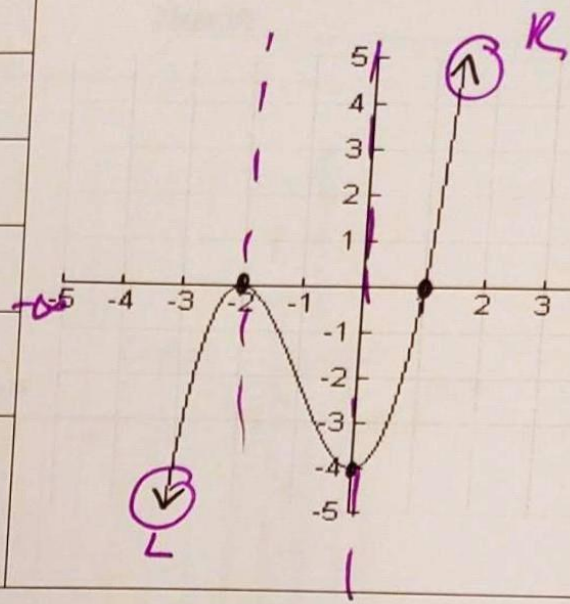
$$\begin{array}{r|rrrr} -5 & 1 & 1 & -17 & 15 \\ & \downarrow & & & \\ & & -5 & 20 & -15 \\ \hline & 1 & -4 & 3 & 0 \end{array}$$

$x^2 - 4x + 3 = 0$

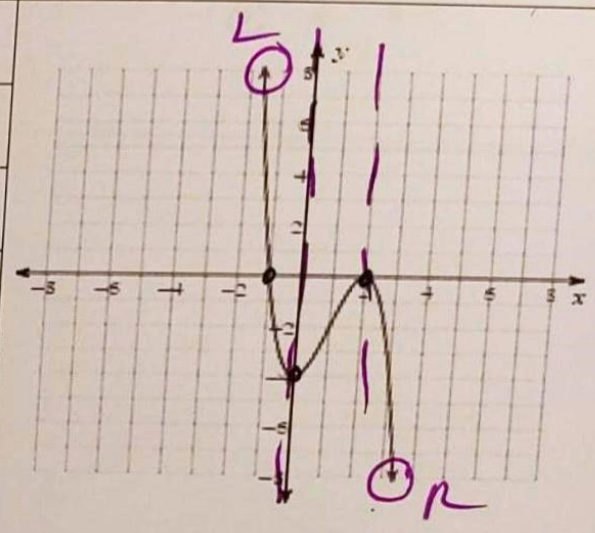
$(x-3)(x-1) = 0$

$x = 3, x = 1, x = -5$

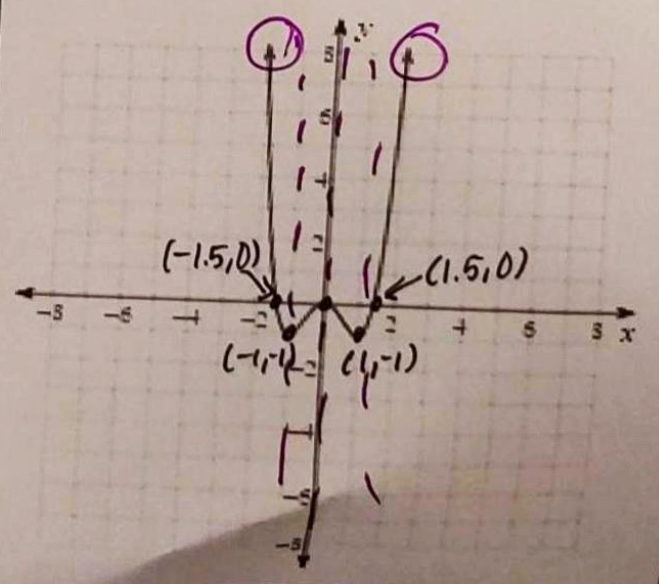
Degree & Name	3 Cubic	Relative Maximum	(-2, 0)
Domain	(-∞, ∞)	Relative Minimum	(0, -4)
Range	(-∞, ∞)	Intervals of Increase	(-2, 0) & (0, ∞)
y-intercept	(0, -4)	Interval of Decrease	(-∞, -2)
x-intercept(s)	(-2, 0), (-1, 0), (1, 0)	Symmetry (even, odd, Neither)	N
Left end behavior	As $x \rightarrow -\infty, y \rightarrow -\infty$		
Right end behavior	As $x \rightarrow \infty, y \rightarrow \infty$		



Degree & Name	3 Cubic	Relative Maximum	(2, 0)
Domain	(-∞, ∞)	Relative Minimum	(0, -4)
Range	(-∞, ∞)	Interval of Increase	(0, 2)
y-intercept	(0, -4)	Intervals of Decrease	(-∞, 0) & (2, ∞)
x-intercept(s)	(-1, 0), (2, 0), (2, 0)	Symmetry (even, odd, Neither)	N
Left end behavior	As $x \rightarrow -\infty, y \rightarrow \infty$		
Right end behavior	As $x \rightarrow \infty, y \rightarrow -\infty$		



Degree & Name	4 Quartic	Relative Maximum	(0, 0)
Domain	(-∞, ∞)	Absolute & Relative Minimum	(-1, -1) & (1, -1)
Range	[-1, ∞)	Intervals of Increase	(-1, 0) & (1, ∞)
y-intercept	(0, 0)	Intervals of Decrease	(-∞, -1) & (0, 1)
x-intercept(s)	(-1.5, 0), (0, 0), (0, 0), (1.5, 0)	Symmetry (even, odd, Neither)	E
Left end behavior	As $x \rightarrow -\infty, y \rightarrow \infty$		
Right end behavior	As $x \rightarrow \infty, y \rightarrow \infty$		



Degree & Name	4 Quartiz	Absolute & Relative Maximum	$(-1, 0)$ & $(1, 0)$
Domain	$(-\infty, \infty)$	Relative Minimum	$(0, 0)$
Range	$(-\infty, 1]$	Intervals of Increase	$(-\infty, -1)$ & $(0, 1)$
y-intercept	$(0, 0)$		
x-intercept(s)	$(-1.5, 0)$, $(0, 0)$, $(0, 0)$, $(1.5, 0)$	Intervals of Decrease	$(-1, 0)$ & $(1, \infty)$
Left end behavior	As $x \rightarrow -\infty, y \rightarrow -\infty$	Symmetry (even, odd, Neither)	\neq
Right end behavior	As $x \rightarrow \infty, y \rightarrow \infty$		

