## Hyperbola

- A Hyperbola is made up of 2 parabolas that are $\qquad$ .
- The denominators of the equation determine how $\qquad$ and $\qquad$ the box is.
- The Vertices of a Hyperbola always lie on the $\qquad$ which always go in the direction of the positive variable.
- The Foci points always lie on the $\qquad$ of the parabolas.


## With Hyperbolas, $\mathrm{a}^{2}$ is always the first denominator!



Graph the following:

$$
\frac{(x-4)^{2}}{25}-\frac{(y+2)^{2}}{4}=1
$$

Center: $\qquad$
$\mathrm{a}^{2}=$ $\qquad$ $\mathrm{a}=$ $\qquad$
$\mathrm{b}^{2}=$ $\qquad$ $\mathrm{b}=$ $\qquad$
Transverse axis: $\qquad$
Vertices:
Co~Vertices:
Foci Distance: $\mathrm{c}^{2}=\mathrm{a}^{2}+\mathrm{b}^{2}$


Foci Points:

Graph the following:

$$
\frac{(y+2)^{2}}{25}-\frac{(x-3)^{2}}{16}=1
$$

Center: $\qquad$
$a^{2}=$ $\qquad$ $\mathrm{a}=$ $\qquad$
$b^{2}=$ $\qquad$ $b=$ $\qquad$

Transverse axis: $\qquad$
Vertices:
Co~Vertices:
Foci Distance: $c^{2}=a^{2}+b^{2}$


Foci Points:

## Writing Equations of a Hyperbola Given

1. Look to see what coordinates change.
$\checkmark \quad$ If the $\mathrm{x} \sim$ coordinates change, the transverse axis will be horizontal ( x is first and $\mathrm{a}^{2}$ will be under $x$ )
$\checkmark \quad$ If the $y \sim$ coordinates change, the transverse axis will be vertical ( $y$ is first and $a^{2}$ will be under y)
2. Find the center.

$$
\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)
$$

3. Find the length of a.
$a=$ center to vertex
Determine $a^{2}$
4. Find the length of c .
$\mathrm{c}=$ center to foci
Determine $c^{2}$
5. Use the formula $c^{2}=a^{2}+b^{2}$ to find the value of $\mathrm{b}^{2}$ by substituting the values of $\mathrm{a}^{2}$ and $\mathrm{c}^{2}$ into the formula. Solve for $b^{2}$.
6. Substitute the values of $a^{2}, b^{2}$, and $(h, k)$ into the formula.

$$
\begin{aligned}
& \frac{(x-h)^{2}}{a^{2}}-\frac{(y-k)^{2}}{b^{2}}=1 \\
& \frac{(y-k)^{2}}{a^{2}}-\frac{(x-h)^{2}}{b^{2}}=1
\end{aligned}
$$

Find the equation of a hyperbola whose vertices are at $(\sim 5,1)$ and $(1,1)$ and whose foci are at $(\sim 6,1)$ and $(2,1)$

Find the equation of a hyperbola whose vertices are at $(\sim 1, \sim 1)$ and $(\sim 1,7)$ and whose foci are at $(\sim 1,8)$ and $(\sim 1, \sim 2)$.

