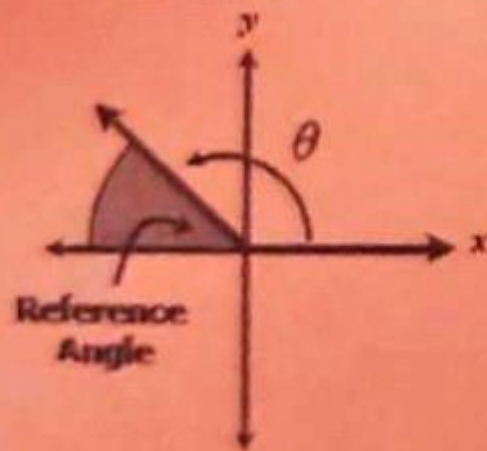


## Reference Angles

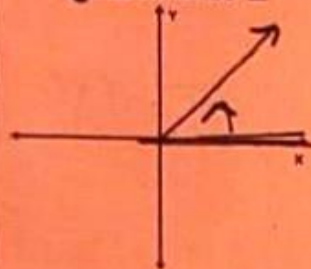


For an angle  $\theta$  in standard form, the reference angle is the positive acute angle formed by the terminal side and the x-axis.

- All reference angles are positive, acute angles measuring between  $0^\circ$  and  $90^\circ$ .
- Finding Reference Angles for Angles greater than  $360^\circ$  or less than  $360^\circ$ 
  1. Find a positive angle less than  $360^\circ$  or  $2\pi$  that is coterminal with the given angle.
  2. Draw  $\theta$  in standard position.
  3. Use the drawing to find the reference angle for the given angle
- When in radians, if the denominator is
  1. 3 the reference angle is  $\pi/3$ .
  2. 4 the reference angle is  $\pi/4$ .
  3. 6 the reference angle is  $\pi/6$ .



### Quadrant 1



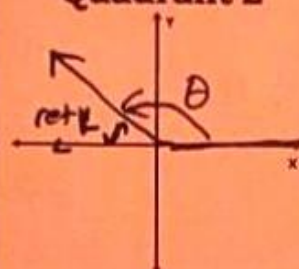
Degrees:

$$\text{ref } L = \theta$$

Radians:

$$\text{ref } L = \theta$$

### Quadrant 2



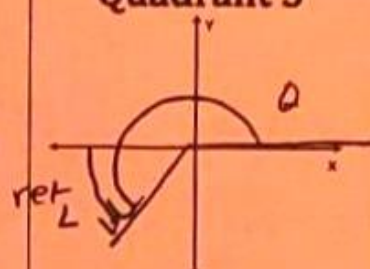
Degrees:

$$\text{ref } L = 180 - \theta$$

Radians:

$$\text{ref } L = \pi - \theta$$

### Quadrant 3



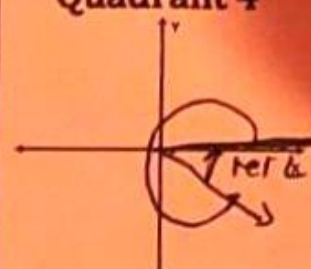
Degrees:

$$\text{ref } L = \theta - 180$$

Radians:

$$\text{ref } L = \theta - \pi$$

### Quadrant 4



Degrees:

$$\text{ref } L = 360 - \theta$$

Radians:

$$\text{ref } L = 2\pi - \theta$$

Directions: Find the reference angle for each angle.

1.  $\theta = 57^\circ$  Q1

$$\boxed{\text{ref } L = 57^\circ}$$

2.  $\theta = 145^\circ$  Q2

$$180 - 145 = 35^\circ$$

$$\boxed{\text{ref } L = 35^\circ}$$

3.  $\theta = 210^\circ$  Q3

$$210 - 180 = 30^\circ$$

$$\boxed{\text{ref } L = 30^\circ}$$

4.  $\theta = 320^\circ$  Q4

$$360 - 320 = 40^\circ$$

$$\boxed{\text{ref } L = 40^\circ}$$

5.  $\theta = -240^\circ$  Q2

$$-240 + 360 = 120^\circ$$

$$\boxed{\text{ref } L = 60^\circ}$$

6.  $\theta = 580^\circ$

$$580 - 360 = 220^\circ$$

$$220 - 180 = 40^\circ$$

$$\boxed{\text{ref } L = 40^\circ}$$

7.  $\theta = \frac{5\pi}{3} = 300^\circ$  Q4

$$360 - 300 = 60^\circ$$

$$\boxed{\text{ref } L = \pi/3}$$

8.  $\theta = \frac{7\pi}{4} = 315^\circ$  Q4

$$360 - 315 = 45^\circ$$

$$\boxed{\text{ref } L = \frac{\pi}{4}}$$

9.  $\theta = -\frac{13\pi}{6} = -390^\circ$

$$-390 + 360 = -30^\circ$$

$$360 - 330 = 30^\circ$$

$$\boxed{\text{ref } L = \pi/6}$$