## Transformations with Matrices

Points on a coordinate plane can be represented by matrices. The ordered pair ( $\mathrm{x}, \mathrm{y}$ ) can be represented by the column matrix

Likewise, polygons can be represented by palcing all of the column matrices of the coordinates of the vertices into one matrix called a $\qquad$ matrix.

Triangle ABC with vertices $\mathrm{A}(3,2), \mathrm{B}(4,-2)$, and $\mathrm{C}(2,-1)$ can be represented by the following vertex matrix.
$\begin{array}{ccc}A & B & C \\ \\ \triangle \mathrm{ABC}=\left[\begin{array}{lll}{[ } & & \end{array}\right]\end{array}$

Matrices can be used to perform transformations. $\qquad$ are functions tht map points of a $\qquad$ onto its $\qquad$ . If the image and preimage are congruent figures, the transformation is an $\qquad$ _.

## Translations:

A $\qquad$ ocurrs when a figure is moved from one location to another without changing its size, shape, or orientation. You can ued matrix addition and a translation matrix to find the coordinates of a translated figure.

Example: Find the coordinates of the vertices of the image of $\Delta \mathrm{ABC}$ with (3,2), $\mathrm{B}(4,-2)$, and $\mathrm{C}(2,-1)$, if it is moved 3 units left, and 1 unit down. Be sure to write out the translation matrix. Then graph $\triangle A B C$ and its image $\triangle A^{\prime} B^{\prime} C^{\prime}$.

## Dilations:

When a geometric figure is enlarged or reduced, the transformation is called a $\qquad$ . You can use scalar multiplication to perform dilations.

Example: Find the coordinates of the vertices of the image of $\triangle A B C$ with (3,2), $B(4,-2)$, and $C(2,-1)$, if it has be reduced by a factor of $1 / 2$. Be sure to write out the dilation matrix. Then graph $\triangle A B C$ and its image $\triangle A^{\prime} B^{\prime} C^{\prime}$


## Reflections:

A $\qquad$ occurs when every point of a figure is mapped to a corresponding image across a line of symmetry using a reflection matrix.

| Reflections |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| For a reflection line <br> over the | x-axis | y-axis | Line $y=x$ | Line $y=-x$ |
| Multiply the vertex <br> matrix on the left by: |  |  |  |  |
| Quick way to check | $(x,-y)$ | $(-x, y)$ | $(y, x)$ | $(y,-x)$ |

Example: Find the coordinates of the vertices of the image $\triangle A B C$ with $(3,2), B(4,-2)$, and $C(2,-1)$. Be sure to write out the reflection matrix. Then graph $\triangle A B C$ and its image $\Delta A^{\prime} B^{\prime} C$.

## a) $x$-axis


c) $y=x$


d) $y=-x$


## Rotations:

A $\qquad$ occurs when a figure is moved around a center point, usually the origin. To determine the vertices of a figure's image by rotation, multiply its vertex matrix by a rotation matrix.

| Rotations |  |  |  |
| :--- | :--- | :--- | :---: |
| For a counterclockwise (CCW) <br> rotation about the origin of | $90^{\circ}$ | $180^{\circ}$ | $270^{\circ}$ |
| Multiply the vertex matrix on the <br> left by: |  |  |  |
| Quick way to check | $(-y, x)$ | $(-x,-y)$ | $(y,-x)$ |
| Same as clockwise (CW) rotation <br> about the origin of | $270^{\circ}$ | Doesn't change | $90^{\circ}$ |

Example: Find the coordinates of the vertices of the image $\triangle A B C$ with $(3,2), B(4,-2)$, and $C(2,-1)$. Be sure to write out the rotation matrix. Then graph $\triangle A B C$ and its image $\triangle A^{\prime} B^{\prime} C$.
a) $90^{\circ} \mathrm{CCW}$
b) $180^{\circ} \mathrm{CCW}$

c) $270^{\circ} \mathrm{CCW}$



